

Figure 3. Adherence of DCA  $k_1$  values to eq 17; closed symbols indicate coincidence of 2-5 independent measurements.

initial data sets had artificially high  $k_1$ 's and were discarded. Corresponding  $k_1$ 's did not change with light exposure and were, therefore, used together with those given in Table I to obtain parameters for  $k_1$  interpolations. It was assumed that  $k_1$  consisted of a temperature and viscosity independent unimolecular decay part,  $k_1^0$ , which is augmented by bimolecular quenching contributions. The  $k_1^0$  value was determined by fitting<sup>32</sup> the  $k_1$ 's to

$$k_1 = k_1^0 + mT/\eta \quad (16)$$

with use of  $T/\eta$  sources given in ref 15:  $k_1^0 = 1576 \pm 20 \text{ s}^{-1}$ ,  $m$

$= (7.96 \pm 0.36) \times 10^{-3} \text{ P}\cdot\text{K}^{-1} \text{ s}^{-1}$ . With  $k_1^0 = 1576 \text{ s}^{-1}$  fixed, the  $k_1$ 's were then fitted<sup>32</sup> to

$$k_1 = k_1^0 + b \exp(-E_q/RT) \quad (17)$$

leading to  $b = (4.75 \pm 0.96) \times 10^4 \text{ s}^{-1}$  and  $E_q = 2.78 \pm 0.12 \text{ kcal/mol}$ , Figure 3. The interpolated  $k_1$  values in Table I were obtained by using eq 17.

The 30-fold increase of  $k_1^0$  relative to the corresponding constant in A is attributed to heavy-atom-enhanced spin-orbit coupling on both the radiative and nonradiative rate constants for the  $T_1 \rightarrow S_0$  transition.<sup>49</sup> Our  $k_1^0$  value, being somewhat lower than that previously reported, falls exactly on a line relating triplet decay rate constants for a series of halogen-substituted anthracenes to spin-orbit coupling factors.<sup>49a</sup> The explanation usually favored for the behavior reflected in the second term of eq 16 or 17 is that it represents quenching by impurities adventitiously present in the solute and/or the solvent.<sup>14,50</sup> Since our measurements were carried out by different investigators over a period of years employing different batches of materials and different purification techniques, we tend to discount this interpretation, unless the impurity is residual oxygen. Diffusion-controlled quenching by an impurity Q would be consistent with  $E_q$  because it is nearly identical with the activation energy for viscous flow in toluene,<sup>15</sup> and would account for  $b$  if  $[Q]$  were  $\sim 5 \times 10^{-8} \text{ M}$ . An alternative interpretation is provided by the self-quenching of  $^3\text{DCA}^*$  by  $^1\text{DCA}$ . With use of  $[\text{DCA}] = 1.15 \times 10^{-4} \text{ M}$ , the value of  $b$  gives  $A = 4.1 \times 10^8 \text{ s}^{-1}$  which is almost identical with  $A_{\text{sq}} = 3.9 \times 10^8 \text{ s}^{-1}$ , the Arrhenius preexponential factor for self-quenching in A.<sup>14</sup> We anticipate testing this interesting possibility by determining the dependence of  $b$  on  $[\text{DCA}]$ .

Registry No. Anthracene, 120-12-7; 9,10-dichloroanthracene, 605-48-1; *cis*-stilbene, 645-49-8; *trans*-stilbene, 103-30-0.

Supplementary Material Available: Table I-S, listing  $k_{\text{obsd}}$  and  $k_{\text{en}}$  values for A (1 page). Ordering information is given on any current masthead page.

## Muonium Addition Reactions to Aromatic Solutes

J. M. Stadlbauer,<sup>†</sup> B. W. Ng, R. Ganti,<sup>‡</sup> and D. C. Walker\*

Contribution from the Chemistry Department, University of British Columbia, Vancouver, Canada V6T 1Y6. Received August 30, 1983

**Abstract:** Reaction rate constants of  $0.3 \times 10^{10}$ – $1.1 \times 10^{10} \text{ M}^{-1} \text{ s}^{-1}$  were determined for the reaction of muonium ( $\mu^+e^-$ , Mu) with seven aromatic solutes in dilute aqueous solution at  $\sim 295 \text{ K}$ . The reaction was deduced to be that of addition to the benzene ring to form cyclohexadienyl radicals. On comparison with the analogous H-atom reactions, the kinetic isotope effects were generally about 3, equal to the mean thermal velocity ratio of Mu/H. When analyzed through the Hammett equation there were serious discontinuities but a small positive  $\rho$  value was evident, not inconsistent with attack by a mildly electron-donating neutral atom forming only free radical intermediates.

A convenient and sensitive method of studying both hydrogen atom reactions and kinetic isotope effects is to study the reactions of muonium (Mu). This is the light atom ( $1/9$  the mass of  $^1\text{H}$ ) which differs from hydrogen in having a positive muon rather than a proton as its nucleus. As the muon is unstable and spin polarized its chemical fate can be investigated by the muon spin rotation method ( $\mu\text{SR}$ ) using nuclear physics counting techniques.<sup>1-3</sup> A

variety of muonium reaction types in aqueous solution have been studied<sup>3,4</sup> including the following: addition, abstraction, substitution, electron spin exchange, redox, and acid-base reactions. For addition reactions, Mu has been observed to add cross  $\text{C}=\text{C}$

\* Address correspondence to this author at the University of British Columbia.

<sup>†</sup> Present address: Department of Chemistry, Hood College, Frederick, MD 21701.

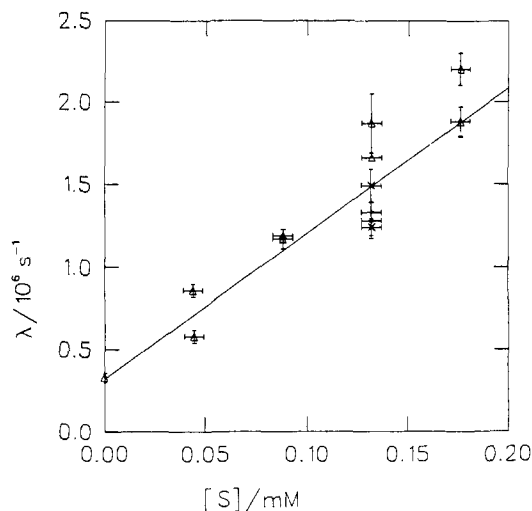
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**Figure 1.** Representative  $\lambda$  vs.  $[S]$  data for aniline. The vertical error bars on each  $\lambda$  value represent the statistical errors, equal to the standard deviation arising from the MINUIT fit to each histogram.

double bonds in aliphatics at rates close to the diffusion-controlled limit of  $\sim 2 \times 10^{10} \text{ M}^{-1} \text{ s}^{-1}$  and across  $\text{C}\equiv\text{N}$  triple bonds of organic solutes some 300-fold slower.<sup>6</sup> Muonium-containing free radicals formed by addition have also been detected directly by  $\mu\text{SR}$  in several pure unsaturated compounds.<sup>7</sup> In the present study an attempt is made to evaluate the factors influencing the mechanism and rate the Mu reactions with substituted benzenes as solutes in dilute aqueous solution at room temperature.

### Experimental Section

Muonium forms when an energetic muon comes to rest in an aqueous sample. Its spin undergoes Larmor precession at a characteristic frequency of  $1.39 \text{ MHz G}^{-1}$  in transverse magnetic fields. Upon decay, a positron is emitted preferentially along the spin vector so that oscillations appear on the ordinary muon lifetime histogram when the positrons are monitored in a given direction within the plane of precession. These oscillations provide an identification of the muonium chemical state, its yield, and a relaxation constant ( $\lambda$ ). The latter is directly related to the bimolecular rate constant ( $k_M$ ) when Mu reacts with a solute  $[S]$ , through  $k_M = (\lambda - \lambda_0)/[S]$ , where  $\lambda_0$  is a "background" component (solvent or apparatus artifact). Details of this  $\mu\text{SR}$  technique, together with the analysis and treatment of data, have been reviewed recently (see, for example, ref 1-3).

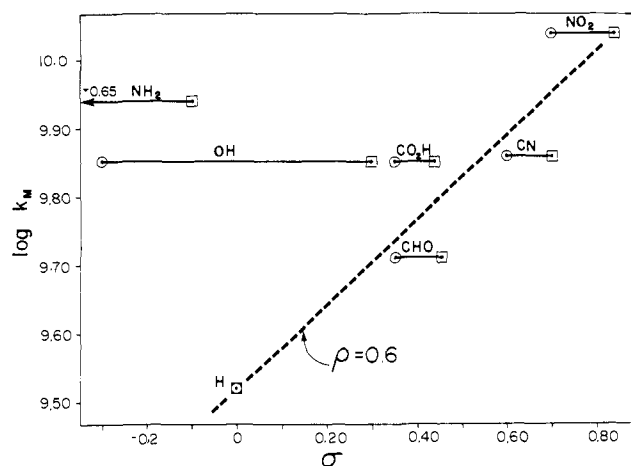
Dilute aqueous solutions of various aromatic solutes were placed in shallow plastic cells and held between the coils of a magnet at the end of the M20 beamline at TRIUMF (the Tri University Meson Facility at the University of B.C.). A field of 8 G was used for the kinetic studies, and spin-polarized "surface" muons with 4.1 MeV of energy were made to strike the aqueous solution through thin (0.05 mm) Mylar windows on the cell. Oxygen needs to be minimized in these solutions because it too reacts rapidly with Mu. For all the solutes studied here, except benzene, the solutions were bubbled with a flow of helium gas during the experiment, and prebubblers containing the same solution reduced the chance of solute loss by evaporation. For the benzene solutions it was necessary to use freeze-pump-thaw cycles together with glass cells and the more penetrating "backward" muon beam.<sup>8</sup> Solutions were made from triply distilled water and Reagent or Spectral Grade compounds.

### Results

Values of  $k_M$  were evaluated from plots of  $\lambda$  vs.  $[S]$ . A typical plot is shown as Figure 1, where some ten individual  $\lambda$  measurements contribute to the value of  $k_M$ . A feeling for the relative magnitude of the statistical errors (shown as error bars) on each  $\lambda$  value compared with the probable error in the evaluated  $k_M$

**Table I.** Muonium Rate Constants ( $k_M$ ) Evaluated for the Reaction of Muonium with Aromatic Solutes in Aqueous Solution at  $\sim 295 \text{ K}$ , from the Measured Values of  $\lambda$  over a Range of  $[S]$

solute	$[S]/\text{mM}$ range	$\lambda/10^6 \text{ s}^{-1}$ range	no. of $\lambda$	$k_M/10^9$ $\text{M}^{-1} \text{ s}^{-1}$
nitrobenzene	0.08-0.24	1.16-3.0	6	11
aniline	0.04-0.18	0.72-2.2	10	8.8
cyanobenzene	0.12-0.20	1.23-1.82	6	7.2
benzoic acid	0.10-0.59	0.91-6 $\pm$ 2	6	7.0
benzaldehyde	0.21-2.0	1.90-9.3	9	5.1
benzene	0.22-0.44	0.90-1.65	3	3.3
[phenol, previously (ref 17)]				7 $\pm$ 2



**Figure 2.** Plot of  $\log k_M$  vs.  $\sigma$  in accordance with the Hammett equation. The meta and para  $\sigma$  values were taken from ref 10 showing the range of  $\sigma_m(\circ)$  and  $\sigma_p(\square)$  reported. The dashed line has a slope (equal to  $\rho$ ) of +0.6.

(variation of slope of line) can be gleaned from this plot. For the seven solutes studied, the ranges of  $[S]$  and  $\lambda$  are given in Table I, together with the  $k_M$  values obtained by least-squares fitting. Realistic errors in  $k_M$  are about  $\pm 25\%$ .

### Discussion

Table I shows that the values obtained for  $k_M$  with these solutes range from  $0.3 \times 10^{10} \text{ M}^{-1} \text{ s}^{-1}$  for unsubstituted benzene to  $1.1 \times 10^{10} \text{ M}^{-1} \text{ s}^{-1}$  for nitrobenzene. Such values fall short by factors of 2 to 6 from the diffusion-controlled limit of  $\sim 2 \times 10^{10} \text{ M}^{-1} \text{ s}^{-1}$  for Mu reactions with solutes of this size in water—as established for efficient redox and spin-exchange reactions.<sup>3,9</sup> They coincide, however, with the range found for Mu addition to vinyl monomers.<sup>5</sup> Apparently the intrinsic reaction rate,  $k_i$  in eq 1,

$$k_M = (k_d^{-1} + k_i^{-1})^{-1} \quad (1)$$

makes the larger contribution to  $k_M$ , perhaps due to loss of aromatic resonance energy, with diffusion ( $k_d$ ) being of secondary importance. These values of  $k_M$  for "addition" reactions are some two orders of magnitude faster than those generally found for "abstraction" or "substitution" reactions for muonium.

The effect of the substituents on  $k_M$  can be discussed with regard to the Hammett linear free energy relationship, eq 2. In this  $k$

$$\log(k/k_0) = \sigma\rho \quad (2)$$

and  $k_0$  are taken as the  $k_M$  values with and without a substituent,  $\sigma$  is the Hammett substituent factor, and  $\rho$  is the reaction constant parameter indicating the susceptibility of the reaction to electronic substituent effects. Figure 2 shows the plot of  $\log k_M$  vs.  $\sigma$ , using the range quoted for  $\sigma_m$  and  $\sigma_p$ .<sup>10</sup> It is clear that no simple

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Table II. Kinetic Isotope Effects ( $k_M/k_H$ ): Comparison of Mu and H Reactions with Solutes in Aqueous Solution at ~295 K

solute	$k_M/10^9$ $M^{-1} s^{-1}$	$k_H^a/10^9$ $M^{-1} s^{-1}$	$k_M/k_H^b$
nitrobenzene	11	3.3	3.3
aniline	8.8	2.9	3.0
cyanobenzene	7.2	0.7	10
benzoic acid	7.0	1	7
phenol	7	2	3.5
benzaldehyde	5.1	1.5	3.4
benzene	3.3	1.1	3.0

<sup>a</sup>  $k_H$  data taken from ref 18. <sup>b</sup> Accumulated errors are difficult to assess but probably range from 20 to 50%.

correlation over the full  $\sigma$  range exists.

If one ignores the substituents with negative  $\sigma$  values (NH<sub>2</sub> and OH) then the remainder show a reasonably linear correlation, as indicated by the dashed line in Figure 2, with a  $\rho$  factor of +0.6. Perhaps alternative, competitive, reaction paths are available to aniline and phenol: indeed, it has been postulated that H atoms "abstract" from these molecules.<sup>11</sup> On the other hand, if one ignored benzene and nitrobenzene instead (the latter on the grounds that H adds to the NO<sub>2</sub> group),<sup>12</sup> then a shallow negatively sloped line would result. Either way, the  $\rho$  factor is very small: not inconsistent with H ( $\rho = -0.45$ )<sup>13</sup> and in sharp contrast with the strongly electron donating character of hydrated electrons (where  $\rho = 4.8$ ).<sup>14</sup> A small  $\rho$  is to be expected for such fast reactions, in accordance with the reactivity-selectivity principle,<sup>15</sup> and it also suggests that the transition states of the reactions have very little polar character. This is consistent with addition by a neutral atom giving free radicals as intermediates in the reaction. It corroborates a previous finding, based on the Brønsted-Bjerrum treatment of ionic atmospheres,<sup>16</sup> that Mu behaves strictly as a neutral atom, showing no tendency to long-range electron or proton (muon) transfer in its reactions in water.

Kinetic isotope effects involving Mu compared to H are multifarious.<sup>3</sup> For the reactions of this study one has the values presented in the last column of Table II. Five out of seven of

them are ca. 3. The ratio of 3 happens to equal the ratio of mean thermal velocities of Mu relative to H from the mass ratio, as in eq 3. This would correspond to the relative encounter frequency

$$\bar{v}_M/\bar{v}_H = (m_H/m_M)^{1/2} \quad (3)$$

(and thus to the preexponential factor in a collision theory interpretation of the Arrhenius equation) if the solvent had no control over diffusion. But, as it is, the kinetic isotope effect has always been found to be unity in the diffusion-controlled limit, suggesting that these atoms behave as Stokes-Einstein particles (where  $D \propto 1/R$ ) in which diffusion is dominated by the solvent rather than the solute.<sup>3,9</sup> This means that the radius of the atom counts but not its mass. An indication of the effective size of H has emerged from recent calculations.<sup>19</sup> As "abstraction" reactions of Mu and H (toward CH<sub>3</sub>OH, for instance) have large inverse isotope effects ( $k_H \gg k_M$ ) due, presumably, to the zero-point energy effect in the activated complexes, perhaps one has in the case of "addition" to the aromatic solutes a fortuitous intermediate stage—with an intrinsic preexponential factor based on velocities. It seems to be neither dominated by the solvent, as in the diffusion-controlled limit, nor dominated by activation in slow reactions where quantum effects take over (tunneling, favoring Mu, or zero-point energy in the transition state, favoring H).

### Conclusions

This study has indicated the value of  $\mu$ SR in elucidating H-atom reactions and kinetic isotope effects. Both H and Mu are of particular interest in chemistry because of their low mass and small size. They are likely to be the first to break the stanglehold (in water, at least) of the Stokes-Einstein restriction on mobility, on the one hand, and the first to show greatly changed probabilities of reaction due to quantum mechanical effects, on the other. It remains to be seen whether the somewhat unsatisfactory concordance with the Hammett equation in Figure 2 arises simply from the variations of reaction types which are possible for Mu and H. However, it is clear that the exceptionally low mass of Mu, which may be a disadvantage in abstraction and substitution reactions, certainly is not in addition, even with respect to the  $\pi$  delocalization of the benzene ring.

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**Registry No.** Muonium, 12587-65-4; nitrobenzene, 98-95-3; aniline, 62-53-3; cyanobenzene, 100-47-0; benzoic acid, 65-85-0; phenol, 108-95-2; benzaldehyde, 100-52-7; benzene, 71-43-2.

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